

# Introduction to Data Structures

Chapter 15

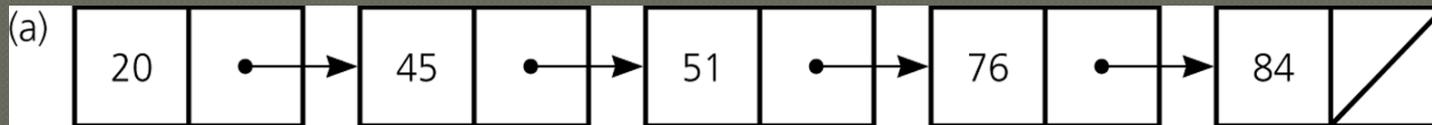
# Linked List

---

- A data structure used for collecting a sequence of objects
- Easy to add and remove elements
- Example
  - Maintaining a list of employees
  - Maintained by name
- Problem with storing in array
  - Shifting when inserting or deleting
- Answer
  - Inserting or deleting in linked list does not require

# Linked List

- Consists of a number of nodes, each of which has a reference to the next node.



# Linked List

---

## ◉ Visiting elements

- Sequential order is effective
- Random order is not effective

# Linked List

---

## Sequence of Nodes

- Node
  - Value or object
  - Reference to next node
- Remove a Node
  - Change the reference
- How do I get to the node
  - List iterator
  - Goes to 1<sup>st</sup> node
  - Goes to node it is pointing to
  - Continues till you get to the node

# Java Class Linked List

---

- ◉ Generic class
- ◉ Must use < >
- ◉ Put the kind of object in < >
- ◉ Use methods to add to beginning and end
- ◉ Traversing the linked list
  - List Iterator

# Creating a Linked List

## Type String

---

- Type String

```
LinkedList<String> students = new  
    LinkedList<String>();
```

Type BankAccounts

```
LinkedList<BankAccount> students = new  
    LinkedList<BankAccount>();
```

# Adding Nodes

## ○ Add first node

```
Students.addLast("Dick");
```

```
Node<Students>  
"Dick"
```

```
Null
```

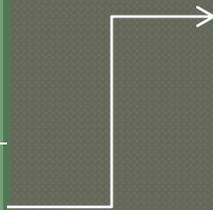
## ○ Add another node after "Dick"

- Student.addLast("Tom");

```
Node<Students>  
"Dick"
```

```
Node<Students>  
"Tom"
```

```
Null
```



# LinkedList Class Methods

---

- ◉ void addFirst(element)
- ◉ void addLast(element)
- ◉ e getFirst( )
- ◉ e getLast( )
- ◉ e removeFirst( )
- ◉ e removeLast( )
  
- ◉ Notice no way to move within list

# ListIterator

---

- listIterator is a method of the LinkedList class.
- Create  
`LinkedListIterator<String>`  
`iterator = students.listIterator();`
- Purpose: to iterate through a list of and visit each element.

# ListIterator

---

- ◉ Begins before the first element.
- ◉ Move Forward
  - `iterator.next( );`
    - Returns the element that the iterator is passing.
    - The type to be returned will depend on the type specified in the `<>`
- ◉ Check to see if there is another element
  - `if (iterator.hasNext());`

# ListIterator

---

## ◉ Add

- `Iterator.add("Kathy");`
- Added after iterator position
- Moves position

## ◉ Remove

- `Iterator.remove()`
- Removes the object that was returned by last call to next or previous

# ListIterator

---

- Careful using the remove method
  - Can be called only once after calling next()
  - Cannot call remove immediately after a call to add.

# LinkedList Class

---

- ◉ Nodes store two links:
  - One to next element
  - One to previous element
- ◉ Doubly linked list
- ◉ For listIterator method
  - Has previous
  - previous

# ListIterator

---

- Traverse entire list

- For each loop

```
For (String name: students)
```

```
{
```

```
    String studentName = name.getName();
```

```
    System.out.println(studentName);
```

```
}
```

# Under the Hood

---

## ◉ Node Class

```
public class Node
{
    public Object data;
    public Node next;
}
```

- data is the object we want to add
- next is the location of the next node

# Under the Hood

---

## ○ Create First or Head

- Pointer to initial element in the linked list
- Initially it will be blank
- Would go in constructor of linked list

```
public LinkedList ( )  
{  
    first = null;  
}
```

# Under the Hood

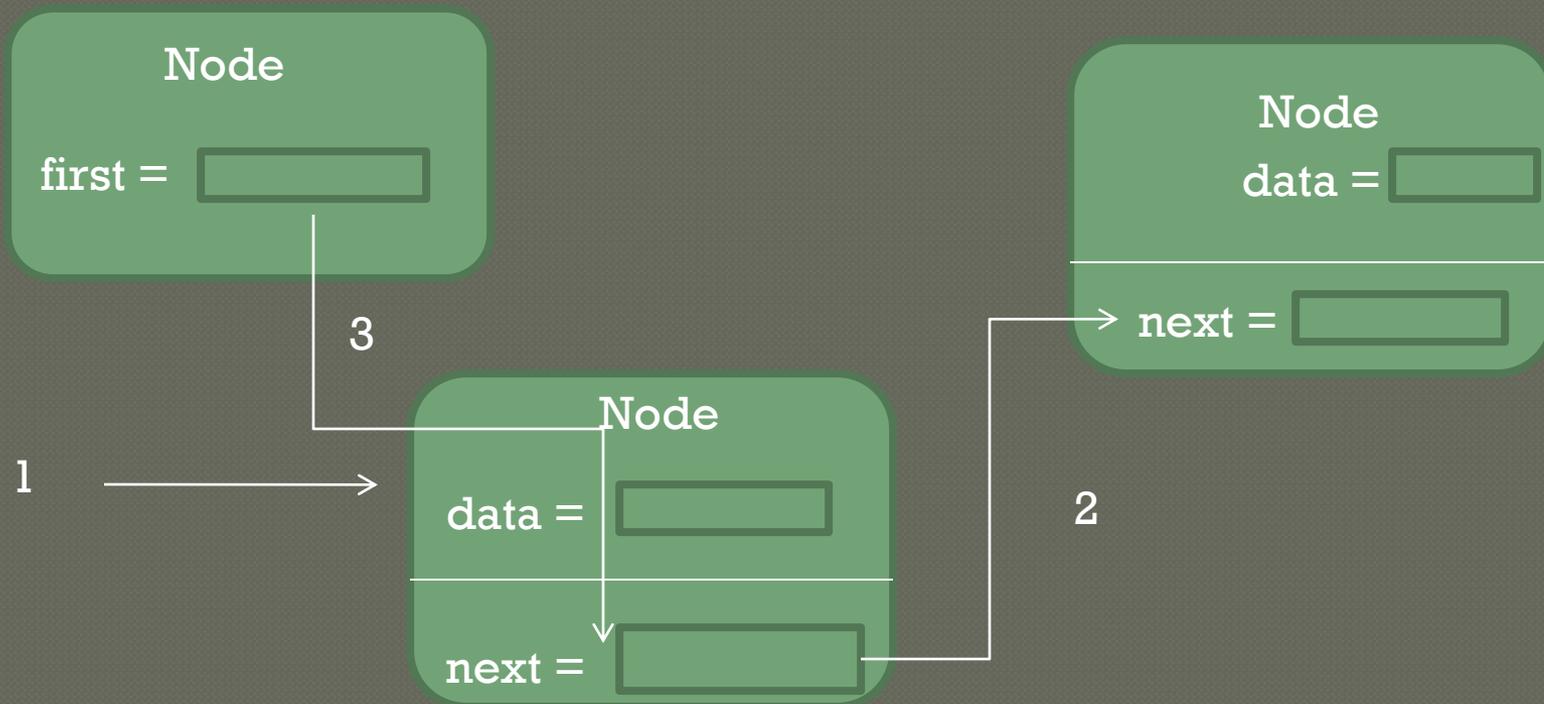
---

- Method to Retrieve First/Head

```
public Object getFirst()
{
    if (first == null)
        throw new NoSuchElementException();
    return first;
}
```

# Under the Hood

- Method to Add First/Head
- Special case
- New list pointer must point to it



# Under the Hood

---

## ◉ Method to Add First/Head

```
public void addFirst(Object element)
{
    Node newNode = newNode();
    newNode.data = element;
    newNode.next = first;
    first = newNode;
}
```

# Under the Hood

---

- Method to Remove first element in the list

```
public void removeFirst()
{
    if (first == null)
        throw new NoSuchElementException();
    Object element = first.data;
    first = first.next();
    return element;
}
```

# Implementing the Iterator Class

---

- ◉ Standard library implements 9 methods we will only implement only 5
- ◉ Iterator class
  - Inner class to LinkedList
  - Has access to private member of LinkedList
  - Has access to first and the private Node class

# Method to define the listIterator

---

```
public ListIterator listIterator()  
{  
    return new LinkedListIterator();  
}
```

# Create the LinkedListIterator

---

```
private class LinkedListIterator
    implements ListIterator
{
    public LinkedListIterator()
    {
        position = null;
        previous = null;
    }
    private Node position;
    private Node previous;
    .....
}
```

# Next Method

---

```
// position is the last visited node.
private class LinkedListIterator
    implements ListIterator
{
    .....
    public Object next()
    {
        if(!hasNext())
            throw new NoSuchElementException
        previous = position; // remember for remove
        if (position == null)
            position = first;
        else
            position = position.next;
        return position.data;
    }
}
```

# hasNext Method

---

```
private class LinkedListIterator
    implement ListIterator
{
    .....
    public boolean hasNext()
    {
        // check for no element after current
        if (position == null)
            return first != null;
        else
            return position.next != null;
    }
}
```

# Remove Method

---

```
public void remove()
{
    if (previous == position)
        throw new IllegalStateException();
    if (position == first)
    {
        removeFirst();
    }
    else
    {
        previous.next = position.next;
    }
    position = previous;
}
```

Remember: position points to the last visited node.  
previous points to the last node before that.

# Set Method

---

```
public void set(Object element)
{
    if (previous == position)
        throw new IllegalStateException();
    position.data = element;
}
```

# Add Method

---

```
public void add(Object element)
{
    if (position == null)
    {
        addFirst(element);
        position = first;
    }
    else
    {
        Node newNode = new Node();
        newNode.data = element;
        newNode.next = position.next;
        position.next = newNode;
        position = newNode;
    }
    previous = position;
}
```

# Abstract and Concrete Data Types

---

## ○ Concrete

- Sequence of node objects with the links between them.

## ○ Abstract

- A linked list is an ordered sequence of data items that can be traversed with a iterator

## ○ Abstract Data Type

- Define the fundamental operations on the data but does not specify an implementation

# Define the Fundamental Operations

---

```
public interface ListIterator
{
    Object next();
    boolean hasNext( );
    void add(Object element);
    void remove( );
    void set(Object element);
    .....
}
```

# Stacks and Queues

---

## ◉ Stack

- Collection of items with “last in first out” retrieval.
- Can insert or remove at the top only
- Can insert in middle

## ◉ Queue

- Collection of times with “first in first out” retrieval.
- Add at the end
- Remove at the top

# Stack

---

- ◉ Stack class in Java Library
- ◉ How to use
  - `Stack <String> s = new Stack<String>();`
  - `s.push()`
  - `s.pop()`
  - `s.peek()`
- ◉ Java class uses an array to implement
- ◉ Can be easily implemented in a linked list

# Checking for Balanced Braces

---

◉ A stack can be used to verify whether a program contains balanced braces

- An example of balanced braces

```
abc{defg{ijk}{l{mn}}op}qr
```

- An example of unbalanced braces

```
abc{def}}{ghij{kl}m
```

# Checking for Balanced Braces

---

- ⦿ Requirements for balanced braces
  - Each time you encounter a “}”, it matches an already encountered “{”
  - When you reach the end of the string, you have matched each “{”

# Checking for Balanced Braces

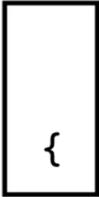
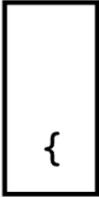
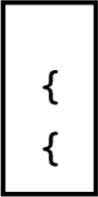
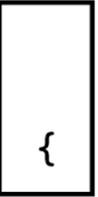
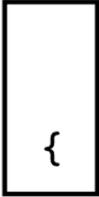
| <u>Input string</u> | <u>Stack as algorithm executes</u>                                                 |                                                                                    |                                                                                   |                                                                                   |                                                                                        |
|---------------------|------------------------------------------------------------------------------------|------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------|-----------------------------------------------------------------------------------|----------------------------------------------------------------------------------------|
|                     | 1.                                                                                 | 2.                                                                                 | 3.                                                                                | 4.                                                                                |                                                                                        |
| {a{b}c}             |   |   |  |  | 1. push "{"<br>2. push "{"<br>3. pop<br>4. pop<br>Stack empty $\implies$ balanced      |
| {a{bc}              |   |   |  |                                                                                   | 1. push "{"<br>2. push "{"<br>3. pop<br>Stack not empty $\implies$ not balanced        |
| {ab}c}              |  |  |                                                                                   |                                                                                   | 1. push "{"<br>2. pop<br>Stack empty when last "}" encountered $\implies$ not balanced |

Figure 7.2

Traces of the algorithm that checks for balanced braces

# Checking for Balanced Braces

---

## ◉ StackException

- A Java method that implements the balanced-braces algorithm should do one of the following
  - Take precautions to avoid an exception
  - Provide `try` and `catch` blocks to handle a possible exception

# Queue

---

- ◉ Queue class in Java Library

- ◉ How to use

- `Queue <Integer> q = new Queue<Integer>();`
- `q.add()` // adds to the tail
- `q.remove()` // removes from the top
- `q.peek()` // get the head of the queue without removing

- ◉ Java class uses an array to implement

- ◉ Can be easily implemented in a linked list

# Queue

---

```
import java.util.LinkedList;
public class LinkedListQueue
{
    public LinkedListQueue()
    {
        list = new LinkedList();
    }
    public void add(Object element)
    {
        list.addLast(element);
    }
    public Object remove()
    {
        return list.removeFirst();
    }
    int size()
    {
        return list.size();
    }
    private LinkedList list;
}
```

# Application: Algebraic Expressions

---

- When the ADT stack is used to solve a problem, the use of the ADT's operations should not depend on its implementation
- To evaluate an infix expressions
  - Convert the infix expression to postfix form
  - Evaluate the postfix expression

# Infix, Prefix and Postfix Expression

# Prefix Notation

---

- ◉ In prefix notation the operator is written before its operands without the use of parentheses or rules of operator precedence.
- ◉ The expression  $(A+B)/(C-D)$  would be written as  $/+AB-CD$  in prefix notation.

# Postfix Notation

---

- Postfix notation is a way of writing algebraic expressions without the use of parentheses or rules of operator precedence.
- The expression  $(A+B)/(C-D)$  would be written as  $AB+CD- /$  in postfix notation.

# Evaluating Postfix Expressions

---

- A postfix calculator
  - Requires you to enter postfix expressions
    - Example: 2, 3, 4, +, \*
  - When an operand is entered, the calculator
    - Pushes it onto a stack
  - When an operator is entered, the calculator
    - Applies it to the top two operands of the stack
    - Pops the operands from the stack
    - Pushes the result of the operation on the stack

# Converting Infix to Postfix

---

- ◎ [http://scriptasylum.com/tutorials/infix\\_postfix/algorithms/infix-postfix/index.htm](http://scriptasylum.com/tutorials/infix_postfix/algorithms/infix-postfix/index.htm)

# Evaluating Postfix Expressions

| <u>Key entered</u> | <u>Calculator action</u>          | <u>Stack (bottom to top)</u> |
|--------------------|-----------------------------------|------------------------------|
| 2                  | push 2                            | 2                            |
| 3                  | push 3                            | 2 3                          |
| 4                  | push 4                            | 2 3 4                        |
| +                  | operand2 = pop stack (4)          | 2 3                          |
|                    | operand1 = pop stack (3)          | 2                            |
|                    | result = operand1 + operand2 (7)  | 2                            |
|                    | push result                       | 2 7                          |
| *                  | operand2 = pop stack (7)          | 2                            |
|                    | operand1 = pop stack (2)          |                              |
|                    | result = operand1 * operand2 (14) |                              |
|                    | push result                       | 14                           |

Figure 7.7

The action of a postfix calculator when evaluating the expression  $2 * (3 + 4)$

# Evaluating Postfix Expressions

---

- To evaluate a postfix expression which is entered as a string of characters
  - Simplifying assumptions
    - The string is a syntactically correct postfix expression
    - No unary operators are present
    - No exponentiation operators are present
    - Operands are single lowercase letters that represent integer values

# to Equivalent Postfix Expressions

---

- An infix expression can be evaluated by first being converted into an equivalent postfix expression
- Facts about converting from infix to postfix
  - Operands always stay in the same order with respect to one another
  - An operator will move only “to the right” with respect to the operands
  - All parentheses are removed

# to Equivalent Postfix Expressions

| <u>ch</u> | <u>stack (bottom to top)</u> | <u>postfixExp</u> |                               |
|-----------|------------------------------|-------------------|-------------------------------|
| a         |                              | a                 |                               |
| -         | -                            | a                 |                               |
| (         | -(                           | a                 |                               |
| b         | -(                           | ab                |                               |
| +         | -( +                         | ab                |                               |
| c         | -( +                         | abc               |                               |
| *         | -( + *                       | abc               |                               |
| d         | -( + *                       | abcd              |                               |
| )         | -( +                         | abcd*             | Move operators                |
|           | -(                           | abcd*+            | from stack to                 |
|           | -                            | abcd*+            | <b>postfixExp</b> until " ( " |
| /         | -/                           | abcd*+            |                               |
| e         | -/                           | abcd*+e           | Copy operators from           |
|           |                              | abcd*+e/-         | stack to <b>postfixExp</b>    |

**Figure 7.8**

A trace of the algorithm that converts the infix expression  $a - (b + c * d) / e$  to postfix form